Supporting Information for the article:

Uncertainties in a carbon footprint model for detergents; quantifying the confidence in a comparative result

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1. Sensitivity Analysis

Methods

In the sensitivity analysis the most influential parameters will be determined. Two methods have been used for the sensitivity analysis. A variance based method called Fourier Amplitude Sensitivity Test (FAST; Saltelli et al. 2000; 2004) and a screening method called the Morris method. Both methods are global sensitivity analysis tools, i.e. the input parameters are varied simultaneously over their full range. Monte Carlo analysis was only used for uncertainty analysis and not used to examine the contribution of the uncertainty in input parameters to the uncertainty in the response variable(s). Simlab is the software used in the sensitivity analysis. It includes the most recent variance-based methods and screening methods for sensitivity analysis besides the more generally known regression based methods (Simlab 2004).

The Morris method is a so-called screening method that uses minimal information to determine the most sensitive parameters. It needs a smaller number of model runs compared to Monte Carlo analysis and FAST. It cannot take into account correlation coefficients among input parameters and a distribution does not have to be specified. The Morris method takes the value ranges of the input parameters as specified by a minimum and maximum and 'jumps' through this parameter space in a number of predefined steps meanwhile measuring the response (elementary effects) of the model. On the basis of the elementary effects a measure of sensitivity is calculated. Two measures are provide μ^* and σ . The μ^* is a measure for overall importance of the parameter. If μ^* of a specific input parameter is higher compared to the μ *'s of other parameters this specific input parameter has a larger contribution to the uncertainty in the response variable than the other input parameters. The σ value can be seen as a measure of non-linear influence of the parameter. The input parameters may be ranked on basis of μ^* and σ but little meaning should be attributed to the absolute value of the sensitivity indices. Also the values for the μ^* and σ cannot be compared between different sensitivity analysis. The method cannot be used for uncertainty analysis.

The FAST method is a variance based method (Saltelli et al. 2004). It needs a larger number of samples compared to Monte Carlo analysis. It can be used for sensitivity and uncertainty analysis. We have compared the results of the uncertainty analysis from the FAST method and the Monte Carlo analysis for a quality check. The FAST method can calculate sensitivity indices for individual parameters but also for groups of parameters. The FAST method was only used to calculate sensitivity indices for groups of parameters and is thus complementary to the Morris method. Using the FAST method for the calculation of sensitivity indices for individual parameters would have needed too much time. The sensitivity indices as calculated by the FAST method may be used quantitatively and used to express the contribution of the input parameter to total uncertainty. The FAST method uses distributions as input and takes into account correlation coefficients.

The results of the FAST analysis are shown in Figure 1 for the Compact Powder. The calculated FAST total indices are plotted as a pie chart illustrating the contribution of the uncertainty in each parameter group to the total uncertainty of the calculated carbon footprint.

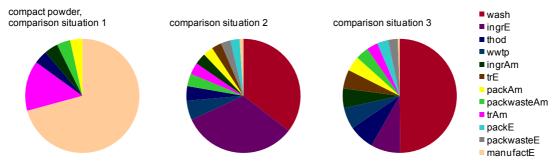


Figure 1: Contribution of the different parameter groups to the total uncertainty of the carbon footprint according to the FAST total indices for the Compact Powder product in comparison situation 1, 2 and 3.

In comparison situation 1, the uncertainty is dominated by uncertainty of the carbon footprint of the detergent manufacturing process and uncertainties of the amount of transport needed. In comparison situation 2 the uncertainty in calculated carbon footprint is dominated by uncertainties in the carbon footprint of chemicals production, the uncertainties in the use phase (efficiency washing machine) and uncertainties with regard to the greenhouse gases emanating from waste water treatment. In comparison situation 3, washing phase, chemicals production and waste water treatment are also dominating the total uncertainty of the calculated carbon footprint.

If we look at the differences between the three comparison situations, the detergent formulation process is dominant in comparison situation 1 and insignificant in comparison situation 2 and 3. The important parameter groups in comparison situation 2 and 3 are quite similar except that uncertainties in the wash phase become even more important.

The importance of the different parameter groups is also reflected in the results of the Morris method, see Table 1. The parameters that belong to groups indicated as important by the FAST method are indicated by grey rows. The most important parameters according the FAST method are always ranked high in every comparison situation according the Morris method. Having two completely different sensitivity analysis method pointing towards the same parameters as being the parameters that contribute mostly to the uncertainty in the carbon footprint increases the reliability of the results of the sensitivity analysis.

An indication of the shape and width of the distribution of the uncertainty of the carbon footprint for the Compact Powder, using the preliminary assessment of the uncertainty in the input parameters, is given in Figure 2. The resulting uncertainty increases going from comparison situation 1 to 3. The shape of the distribution is slightly skewed.

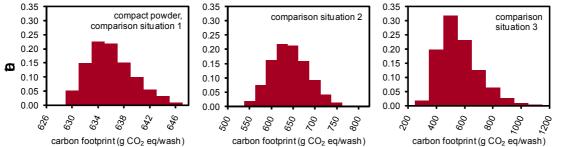


Figure 2: Shape and width of the uncertainty distribution of the carbon footprint for the Compact Powder product calculated with Monte Carlo analysis.

Table 1: Results of the sensitivity analysis using the Morris method for the Compact Powder product for comparison situation 1, 2 and 3. The Morris Index, μ^* , is shown which is a measure of the total importance of a parameter. Grey rows indicate parameters that belong to a group which is important according the FAST analysis, see Figure 1. Only the top twenty most important input parameters are shown.

Comparison situation	1	Comparison situati	on 2	Comparison situa	ation 3
parameter	μ*	parameter	μ*	parameter	μ*
manufactE	9.8462	washElek	97.9106	tempToggle	360.42
trrawrtopoAm	4.0848	zeoliteE	66.3323	ElekE	325.9625
trrawrtoplAm	0.8173	carbonateE	27.4692	wwtpToggle	121.8669
trfinrAm	0.793	einorgwwtp	19.0672	zeoliteE	64.2605
zeoliteAm	0.5285	nalasE	18.8316	washElek	40.3287
corruAm	0.5196	percarbonateE	18.5065	carbonateE	23.7292
carbonateAm	0.4756	taedE	18.0145	nalasE	19.434
nalasAm	0.3492	co2wwtp	16.3023	taedE	18.5853
percarbonateAm	0.3491	manufactE	9.8462	percarbonateE	17.9592
trrawstoplAm	0.3401	eorgwwtp	8.1342	manufactE	9.2611
corrulandfAm	0.3289	truckE	6.1656	einorgwwtp	8.1087
thnalas	0.3187	ae7E	5.708	co2wwtp	6.8747
waterAm	0.12	ch4wwtp	4.4112	ae7E	5.8935
taedAm	0.1161	trrawrtopoAm	3.7168	truckE	3.965
ae7Am	0.0927	corruE	2.9299	eorgwwtp	3.4629
thtaed	0.0923	citricE	2.5017	ch4wwtp	3.0299
ldpeAm	0.0867	cmcE	1.6062	trrawrtopoAm	2.8359
thae7	0.0846	acrylicE	1.4261	citricE	2.8074
corrureAm	0.0789	k1clE	1.0406	corruE	2.6258
sulfateAm	0.0622	hedpE	0.967	wasteToggle	2.5601

The results of the sensitivity analysis for the Ultra Liquid product using the FAST method is given in Figure 3. In comparison situation 1 the uncertainty in the carbon footprint is mainly caused by uncertainties in the transport amounts used in the model and emissions during formulation of the detergent. Compared to the Compact Powder product, emissions during formulation of the detergent have become much less important. This is likely the result of the large difference in emissions during the formulation of the CO2 eq/kg) and Ultra Liquid (44 g CO2 eq/kg).

In comparison situation 2 and 3 the parameter groups that contribute most to the uncertainty of the carbon footprint are the wash phase, emissions in the waste water treatment and emissions during the production of chemicals for the detergent. However, compared to the Compact Powder product the importance of waste water treatment and chemicals production is not so clear cut. Differences between second third, fourth and fifth in rank are small. There is another difference between the Ultra Liquid product and the Compact Powder product. While in the Compact Powder product the importance of the wash phase increased relatively going from comparison situation 2 to 3, for the Ultra Liquid product it decreases.

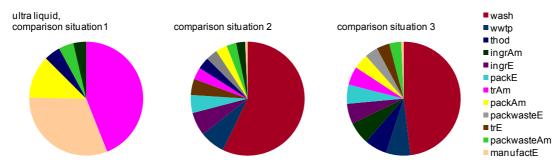


Figure 3: Contribution of the different parameter groups to the total uncertainty of the carbon footprint according to FAST total indices for Ultra Liquid in comparison situation 1, 2 and 3.

The distribution of uncertainties calculated for the Ultra Liquid product, using the preliminary assignment of uncertainties is shown in Figure 4. Just like the Compact Powder case, uncertainties increase going from comparison situation 1 to 3. The shape of the distribution is slightly skewed.

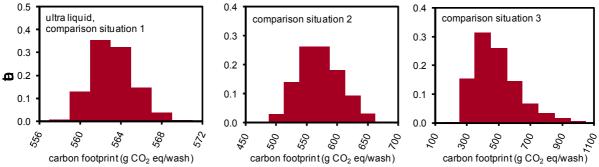


Figure 4: Shape and width of the uncertainty distribution of the carbon footprint for Ultra Liquid calculated with Monte Carlo analysis.

The results of the Morris method corroborate the findings of the FAST method except that the differences between the Morris sensitivity indexes for the parameters are not so big, see Table 2. For instance, in comparison situation 1 the amount of HDPE (packaging material) that goes into Ultra Liquid packaging (hdpeAm) scores quite high while the FAST index for the group of parameters describing the amount of package material (packAm) is ranked third. Grey rows indicate input parameters that belong to a parameter group indicated as most important according to the FAST analysis.

Table 2: Results of the sensitivity analysis using the Morris method for the Ultra Liquid product for comparison situation 1, 2 and 3. The Morris Index, μ^* , is shown which is a measure of the total importance of a parameter. Grey rows indicate parameters that belong to a group which is important according to the FAST analysis, see Figure 3. Only the top twenty of most important parameters is shown.

Comparison situatio	n 1	Comparison situat	ion 2	Comparison situ	ation 3
parameter	μ*	parameter	μ*	parameter	μ*
trrawtopoAm	4.6794	washElek	94.5887	ElekE	317.577
manufactE	3.5223	co2wwtp	23.7134	tempToggle	269.2361
hdpeAm	1.7064	einorgwwtp	18.7587	wwtpToggle	157.6786
trrawrtoplAm	0.8838	nalasE	15.3045	washElek	46.972
corrulandfAm	0.7658	hdpeE	12.9363	nalasE	16.2663
corruAm	0.586	c14ae7E	11.952	hdpeE	16.116
nalasAm	0.4846	eorgwwtp	11.5858	einorgwwtp	11.615
trrawstoplAm	0.3897	truckE	8.5799	c14ae7E	11.5864
c14ae7Am	0.3258	soapE	7.6782	soapE	8.0906
ppAm	0.2976	metaborateE	7.6756	truckE	7.8073
thnalas	0.2663	ch4wwtp	6.31	metaborateE	7.7146
waterAm	0.2434	citrateE	5.8275	citrateE	6.0159
soapAm	0.2232	c12aesE	4.8761	eorgwwtp	5.7845
corrureAm	0.1936	propglycolE	4.2059	wasteToggle	5.7513
thc14ae7	0.166	manufactE	3.8459	c12aesE	5.3565
c12aesAm	0.1515	trrawtopoAm	3.394	co2wwtp	4.738
thsoap	0.1264	ehdqE	2.4598	propglycolE	4.4656
meaborateAm	0.123	corrulandfE	2.4169	manufactE	3.8459
citrateAm	0.1063	ppE	2.2953	trrawtopoAm	3.8313
hdpeinceAm	0.1025	corruE	1.7884	ch4wwtp	3.8218

Concluding given our preliminary assessment of the uncertainty of the input parameters, the parameters that have the largest contribution to uncertainty in the response variable are quite similar for the Compact Powder and Ultra Liquid product. In comparison situation 1, the parameters with the largest contribution are the carbon footprint of detergent formulation and transport distances. In comparison situation 2, efficiency of the washing machine, carbon footprint of chemicals production and waste water treatment are the largest contributors to the uncertainty of the carbon footprint. These are also the input parameters with the largest contribution situation 3, but with a different magnitude.

2. Uncertainty specification input parameters Compact Powder

				mathematica	description	
Stage	parameter	mean	unit	distribution	μ	σ
		value				
product ingredient	amount ingredients	Nondisclose	d Information	Nondisclosed	I Information	
production						
packaging	amount LDPE in package and bulk pack	5.93	g/wash	log normal	1.779	0.04766
production		98.71	g/wash	l °	4.591	0.04766
	amount Corrugate in package and bulk pack	90.71	g/wash	log normal	4.591	0.04766
transport	distance transport raw material, road to port, by truck	500	km	log normal	6.137	0.3931
	distance transport raw material, sea to plant, by ship	100	km	log normal	4.528	0.3931
	distance transport raw material, road to plant, by truck	100	km	log normal	4.528	0.3931
	distance transport finished product, road in UK (to oxford), by truck	100	km	log normal	4.528	0.3931
formula	emissions during formulation compact powder	129	g CO2 eq/kg	log normal	4.783	0.3931
manufacturing		120	g 002 cq/kg		4.700	0.0001
n a cha cin a succeta		0.1			-2.311	0.1312
packaging waste treatment	fraction recycling of LDPE in package and bulk pack	-	-	log normal		
louinon	fraction recycling of Corrugate in package and bulk pack	0.37	-	log normal	-1.003	0.1312
	fraction packaging landfilling of LDPE in package and bulk pack	0.911	-	log normal	-0.1018	0.1312
	fraction packaging incineration with energy recovery of LDPE in package and	0.088	-	log normal	-2.439	0.1312
	bulk pack fraction packaging incineration w/o energy recovery of LDPE in package and	0.001	-	log normal	-6.916	0.1312
	bulk pack fraction packaging landfilling of Corrugate in package and bulk pack	0.911	_	log normal	-0.1018	0.1312
			-	Ŭ		
	fraction packaging incineration with energy recovery of Corrugate in package and bulk pack	0.088	-	log normal	-2.439	0.1312
	fraction packaging incineration w/o energy recovery of Corrugate in package and bulk pack	0.001	-	log normal	-6.916	0.1312

waste water	Theoretical oxygen of ingredients	Non disclosed information	Non disclosed information
treatment			

Compact Powder: 0	Comparison situation 2			mathem	lon-disclosed information og normal 1.779 og normal 4.591 og normal 7.566 og normal 6.234	
		mean	unit		· · ·	σ
Stage	parameter	value				
use	energy use washing machine (a measure of efficiency)	0.0168	kWh/ºC.wash	normal	0.01680	0.005450
product ingredient production	amount ingredients	Non-disclosed inform	nation	Non-disclosed info	rmation	
packaging production	amount LDPE in package and bulk pack	5.93	g/wash	log normal	1.779	0.04766
production	amount Corrugate in package and bulk pack	98.71	g/wash	log normal	4.591	0.04766
	emission during production LDPE for package and bulk pack	2086.3	g CO2 eq/package	log normal	7.566	0.3931
	emission during production Corrugate for package and bulk pack		g CO2 eq/package	log normal	6.234	0.3931
transport	distance transport raw material, road to port, by truck	500	km	log normal	6.137	0.3931
	distance transport raw material, sea to plant, by ship	100	km	log normal	4.528	0.3931
	distance transport raw material, road to plant, by truck	100	km	log normal	4.528	0.3931
	distance transport finished product, road in UK (to oxford), by truck	100	km	log normal	I 7.566 I 6.234 I 6.137 I 4.528 I 4.528 I 4.528 I 4.528	0.3931
	emissions during transport by truck	107.118	g CO2 eq/ton.km	log normal	4.597	0.3931
	emissions during transport by ship	44.5794	g CO2 eq/ton.km	log normal	3.720	0.3931
formula manufacturing	emissions during formulation compact powder	129	g CO2 eg/kg	log normal	4.783	0.3931
packaging waste treatment	fraction recycling of LDPE in package and bulk pack fraction recycling of Corrugate in package and bulk pack	0.1 0.37		log normal log normal	-2.311 -1.003	0.1312 0.1312

	fraction packaging landfilling of LDPE in package and bulk pack fraction packaging incineration with energy recovery of LDPE in package and	0.911	-	log normal	-0.1018	0.1312
	bulk pack fraction packaging incineration w/o energy recovery of LDPE in package and	0.088	-	log normal	-2.439	0.1312
	bulk pack	0.001	-	log normal	-6.916	0.1312
	fraction packaging landfilling of Corrugate in package and bulk pack	0.911	-	log normal	-0.1018	0.1312
	fraction packaging incineration with energy recovery of Corrugate in package and bulk pack fraction packaging incineration w/o energy recovery of Corrugate in package	0.088	-	log normal	-2.439	0.1312
	and bulk pack	0.001	-	log normal	-6.916	0.131
	emissions during recycling of LDPE in package and bulk pack	56	g CO2 eq/package	log normal	3.948	0.393
	emissions during recycling of Corrugate in package and bulk pack	576.79	g CO2 eq/package	log normal	6.280	0.3931
	emissions during incineration with energy recovery of LDPE	1874.001	g CO2 eq/package	log normal	7.459	0.393
	emissions during incineration w/o energy recovery of LDPE	2904.84	g CO2 eq/package	log normal	7.897	0.393
	emissions during landfilling of LDPE	6.15	g CO2 eq/package	log normal	1.739	0.393
	emissions during incineration with energy recovery of Corrugate	-377.02	g CO2 eq/package	log normal	5.855	0.393
	emissions during incineration w/o energy recovery of Corrugate	41.1744	g CO2 eq/package	log normal	3.641	0.393
	emissions during landfilling of Corrugate	1198.47	g CO2 eq/package	log normal	7.012	0.3931
waste water treatment	Theoretical oxygen demand of ingredients	Non-disclosed inform	nation	Non-disclosed in	formation	
	electricity use per kg inorganic material in WWTP	0.65	kWh/kg	log normal	-0.5080	0.393
	natural gas use per kg inorganic material in WWTP	0.0211	m3/kg	log normal	-3.936	0.393
	diesel oil use per kg inorganic material in WWTP	0.011	g/kg	log normal	-4.587	0.393
	electricity use per kg COD organic material in WWTP	0.29	kWh/kg COD	log normal	-1.315	0.393
	natural gas use per kg COD organic material in WWTP	0.0093	cum/kg COD	log normal	-4.755	0.393
	diesel oil use per kg COD organic material in WWTP	0.005	g/kg COD	log normal	-5.376	0.393
		1				
	emission of CO2 in WWTP	577.2	g CO2/kg COD	log normal	6.332	0.227

Compact Powder:	Comparison situation 3					
				mathema	tical description	n
Stage	parameter	value	unit	distribution	μ	σ
use	washing temperature	30/40		discrete uniform	n.a.	n.a.
	energy use washing machine (a measure of efficiency)	0.0168	kWh/ºC.wash	normal	0.01680	0.005450
	emissions during electricity generation for washing machine	570	g CO2 eq/kWh	log normal	6.326	0.1982
product ingredient production	amount ingredients	Non-disclosed informa	tion	Non-disclosed infor	mation	
packaging	amount LDPE in package and bulk pack	5.93	g/wash	log normal	1.779	0.04766
production	amount Corrugate in package and bulk pack	98.71	g/wash	log normal	4.591	0.04766
	emission during production LDPE for package and bulk pack	2086.3	g CO2 eq/package	log normal	7.566	0.3931
	emission during production Corrugate for package and bulk pack	550.98	g CO2 eq/package	log normal	6.234	0.3931
transport	distance transport raw material, road to port, by truck	500	km	log normal	6.137	0.3931
	distance transport raw material, sea to plant, by ship	100	km	log normal	4.528	0.3931
	distance transport raw material, road to plant, by truck	100	km	log normal	4.528	0.3931
	distance transport finished product, road in UK (to oxford), by truck	100	km	log normal	4.528	0.3931
	emissions during transport by truck	107.118	g CO2 eq/ton.km	log normal	4.597	0.3931
	emissions during transport by ship	44.5794	g CO2 eq/ton.km	log normal	3.720	0.3931
formula manufacturing	emissions during formulation compact powder	129	g CO2 eq/kg	log normal	4.783	0.3931
packaging waste treatment	waste treatment package material	yes/no	-	discrete uniform	n.a.	n.a.
	fraction recycling of LDPE in package and bulk pack fraction recycling of Corrugate in package and bulk pack	0.1 0.37		log normal log normal	-2.311 -1.003	0.1312 0.1312

1		1		1		1
	fraction packaging landfilling of LDPE in package and bulk pack fraction packaging incineration with energy recovery of LDPE in package and	0.911	-	log normal	-0.1018	0.1312
	bulk pack fraction packaging incineration w/o energy recovery of LDPE in package and	0.088	-	log normal	-2.439	0.1312
	bulk pack	0.001	-	log normal	-6.916	0.1312
	fraction packaging landfilling of Corrugate in package and bulk pack fraction packaging incineration with energy recovery of Corrugate in package	0.911	-	log normal	-0.1018	0.1312
	and bulk pack fraction packaging incineration w/o energy recovery of Corrugate in package	0.088	-	log normal	-2.439	0.1312
	and bulk pack	0.001	-	log normal	-6.916	0.1312
	emissions during recycling of LDPE in package and bulk pack	56	g CO2 eq/package	log normal	3.948	0.3931
	emissions during recycling of Corrugate in package and bulk pack	576.79	g CO2 eq/package	log normal	6.280	0.3931
	emissions during incineration with energy recovery of LDPE	1874.001	g CO2 eq/package	log normal	7.459	0.3931
	emissions during incineration w/o energy recovery of LDPE	2904.84	g CO2 eq/package	log normal	7.897	0.3931
	emissions during landfilling of LDPE	6.15	g CO2 eq/package	log normal	1.739	0.3931
	emissions during incineration with energy recovery of Corrugate	-377.02	g CO2 eq/package	log normal	5.855	0.3931
	emissions during incineration w/o energy recovery of Corrugate	41.1744	g CO2 eq/package	log normal	3.641	0.3931
	emissions during landfilling of Corrugate	1198.47	g CO2 eq/package	log normal	7.012	0.3931
waste water	waste water treatment plant	yes/no	-	discrete uniform	n.a. n	i.a.
treatment	Theoretical oxygen demand of ingredients	Non-disclosed informa	tion	Non-disclosed info	ormation	
	electricity use per kg inorganic material in WWTP		kWh/kg	log normal	-0.5080	0.3931
	natural gas use per kg inorganic material in WWTP	1	m3/kg	log normal	-3.936	0.3931
	diesel oil use per kg inorganic material in WWTP electricity use per kg COD organic material in WWTP	0.011	g/kg kWh/kg COD	log normal log normal	-4.587 -1.315	0.3931 0.3931
			cum/kg COD	°		0.3931
	natural gas use per kg COD organic material in WWTP diesel oil use per kg COD organic material in WWTP		g/kg COD	log normal log normal	-4.755 -5.376	0.3931
	emission of CO2 in WWTP	577.2	g CO2/kg COD	log normal	6.332	0.2272
	emission of CH4 in WWTP	6.56	g CO2/kg COD	log normal	1.855	0.2272

3. Uncertainty specification input parameters Ultra Liquid

				mathematica	I description	
Stage	parameter	mean	unit	distribution	μ	σ
		value				
product	amount ingredients	Non-disclosed inf	ormation	Non-disclose	d information	
ingredient production						
packaging	amount HDPE in package and bulk pack	68.5	g/wash	log normal	4.226	0.04766
production	amount PP in package and bulk pack	10	g/wash	log normal	2.301	0.04766
	amount LDPE in package and bulk pack	0.688888889	g/wash	log normal	-0.3738	0.04766
	amount Corrugate in package and bulk pack	62.85555556	g/wash	log normal	4.140	0.04766
transport	distance transport raw material, road to port, by truck	500	km	log normal	6.137	0.3931
	distance transport raw material, sea to plant, by ship	100	km	log normal	4.528	0.3931
	distance transport raw material, road to plant, by truck	100	km	log normal	4.528	0.3931
formula manufacturing	emissions during formulation compact powder	44	g CO2 eq/kg	log normal	3.707	0.3931
packaging waste	fraction recycling of HDPE in package and bulk pack	0.5	-	log normal	-0.7018	0.1312
treatment	fraction recycling of LDPE in package and bulk pack	0.1	-	log normal	-2.311	0.1312
	fraction recycling of Corrugate in package and bulk pack	0.37	-	log normal	-1.003	0.1312
	fraction packaging landfilling of HDPE in package and bulk pack	0.911	-	log normal	-0.1018	0.1312
	fraction packaging incineration with energy recovery of HDPE in package and bulk pack	0.088	-	log normal	-2.439	0.1312
	fraction packaging incineration w/o energy recovery of HDPE in package and bulk pack	0.001	-	log normal	-6.916	0.1312
	fraction packaging landfilling of PP in package and bulk pack	0.911	-	log normal	-0.1018	0.1312
	fraction packaging incineration with energy recovery of PP in package and bulk pack	0.088	-	log normal	-2.439	0.1312
	fraction packaging incineration w/o energy recovery of PP in package and bulk pack	0.001	-	log normal	-6.916	0.1312
	fraction packaging landfilling of LDPE in package and bulk pack	0.911	-	log normal	-0.1018	0.1312

treatment			nauon			
waste water	Theoretical oxygen demand ingredients	Non-disclosed inforr	mation	Non-disclosed	information	
	fraction packaging incineration with energy recovery of Corrugate in package and bulk pack fraction packaging incineration w/o energy recovery of Corrugate in package and bulk pack	0.088 0.001	-	log normal	-2.439 -6.916	0.1312 0.1312
	fraction packaging incineration w/o energy recovery of LDPE in package and bulk pack fraction packaging landfilling of Corrugate in package and bulk pack	0.001 0.911	-	log normal log normal	-6.916 -0.1018	0.1312 0.1312
	fraction packaging incineration with energy recovery of LDPE in package and bulk pack	0.088	-	log normal	-2.439	0.1312

				mathematica	mathematical description		
Stage	parameter	mean	unit	distribution	μ	σ	
		value					
use	energy use washing machine (a measure of efficiency)	0.0168	kWh/ºC.wash	normal	0.01680	0.005450	
product ingredient production	amount ingredients	Non-disclosed inf	ormation	Non-disclose	d information		
packaging	amount HDPE in package and bulk pack	68.5	g/wash	log normal	4.226	0.04766	
production	amount PP in package and bulk pack	10	g/wash	log normal	2.301	0.04766	
	amount LDPE in package and bulk pack	0.688888889	g/wash	log normal	-0.3738	0.04766	
	amount Corrugate in package and bulk pack	62.85555556	g/wash	log normal	4.140	0.04766	
	emission during production HDPE for package and bulk pack	3700	g CO2 eq/package	log normal	8.139	0.3931	
	emission during production PP for package and bulk pack	4400	g CO2 eq/package	log normal	8.312	0.3931	
	emission during production LDPE for package and bulk pack	2086.3	g CO2 eq/package	log normal	7.566	0.3931	
	emission during production Corrugate for package and bulk pack	550.98	g CO2 eq/package	log normal	6.234	0.3931	
transport	distance transport raw material, road to port, by truck	500	km	log normal	6.137	0.3931	

	distance transport raw material, sea to plant, by ship	100	km	log normal	4.528	0.3931
	distance transport raw material, road to plant, by truck	100	km	log normal	4.528	0.3931
	emissions during transport by truck	107.118	g CO2 eq/ton.km	log normal	4.597	0.3931
	emissions during transport by ship	44.5794	g CO2 eq/ton.km	log normal	3.720	0.3931
formula manufacturing	emissions during formulation compact powder	44	g CO2 eq/kg	log normal	3.707	0.3931
packaging waste	fraction recycling of HDPE in package and bulk pack	0.5		log normal	-0.7018	0.1312
treatment	fraction recycling of LDPE in package and bulk pack	0.1	-	log normal	-0.7018	0.1312
	fraction recycling of Corrugate in package and bulk pack	0.1	-	log normal	-2.311	0.1312
		0.57	-	log normal	-1.005	0.1312
	fraction packaging landfilling of HDPE in package and bulk pack	0.911	-	log normal	-0.1018	0.1312
	fraction packaging incineration with energy recovery of HDPE in package and	0.088	-	log normal	-2.439	0.1312
	bulk pack fraction packaging incineration w/o energy recovery of HDPE in package and bulk pack	0.001	-	log normal	-6.916	0.1312
	fraction packaging landfilling of PP in package and bulk pack	0.911	-	log normal	-0.1018	0.1312
	fraction packaging incineration with energy recovery of PP in package and bulk	0.088	-	log normal	-2.439	0.1312
	pack fraction packaging incineration w/o energy recovery of PP in package and bulk pack	0.001	-	log normal	-6.916	0.1312
	fraction packaging landfilling of LDPE in package and bulk pack	0.911	-	log normal	-0.1018	0.1312
	fraction packaging incineration with energy recovery of LDPE in package and bulk pack	0.088	-	log normal	-2.439	0.1312
	fraction packaging incineration w/o energy recovery of LDPE in package and bulk pack	0.001	-	log normal	-6.916	0.1312
	fraction packaging landfilling of Corrugate in package and bulk pack	0.911	-	log normal	-0.1018	0.1312
	fraction packaging incineration with energy recovery of Corrugate in package and bulk pack	0.088	-	log normal	-2.439	0.1312
	fraction packaging incineration w/o energy recovery of Corrugate in package and bulk pack	0.001	-	log normal	-6.916	0.1312
	emissions during recycling of HDPE in package and bulk pack	56	g CO2 eq/package	log normal	3.948	0.3931
	emissions during recycling of LDPE in package and bulk pack	56	g CO2 eq/package	log normal	3.948	0.3931
	emissions during recycling of Corrugate in package and bulk pack	576.79	g CO2 eq/package	log normal	6.280	0.3931
	emissions during incineration with energy recovery of HDPE	1874.001	g CO2 eg/package	log normal	7.459	0.3931
	emissions during incineration w/o energy recovery of HDPE	2904.84	g CO2 eq/package	log normal	7.897	0.3931

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	emissions during landfilling of HDPE	6.15	g CO2 eq/package	log normal	1.739	0.3931
	emissions during incineration with energy recovery of PP	1675.48	g CO2 eq/package	log normal	7.347	0.3931
	emissions during incineration w/o energy recovery of PP	2904.84	g CO2 eq/package	log normal	7.897	0.3931
	emissions during landfilling of PP	6.15	g CO2 eq/package	log normal	1.739	0.3931
	emissions during incineration with energy recovery of LDPE	1874.001	g CO2 eq/package	log normal	7.459	0.3931
	emissions during incineration w/o energy recovery of LDPE	2904.84	g CO2 eq/package	log normal	7.897	0.3931
	emissions during landfilling of LDPE	6.15	g CO2 eq/package	log normal	1.739	0.3931
	emissions during incineration with energy recovery of Corrugate	-377.02	g CO2 eq/package	log normal	5.855	0.3931
	emissions during incineration w/o energy recovery of Corrugate	41.1744	g CO2 eq/package	log normal	3.641	0.3931
	emissions during landfilling of Corrugate	1198.47	g CO2 eq/package	log normal	7.012	0.3931
waste water treatment	Theoretical oxygen demand of ingredients	Non-disclosed i	Non-disclosed information No		d information	,
	electricity use per kg inorganic material in WWTP	0.65	kWh/kg	log normal	-0.5080	0.3931
	natural gas use per kg inorganic material in WWTP	0.0211	m3/kg	log normal	-3.936	0.3931
	diesel oil use per kg inorganic material in WWTP	0.011	g/kg	log normal	-4.587	0.3931
	electricity use per kg COD organic material in WWTP	0.29	kWh/kg COD	log normal	-1.315	0.3931
	natural gas use per kg COD organic material in WWTP	0.0093	cum/kg COD	log normal	-4.755	0.3931
	diesel oil use per kg COD organic material in WWTP	0.005	g/kg COD	log normal	-5.376	0.3931
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	emission of CO2 in WWTP	577.2	g CO2/kg COD	log normal	6.332	0.2272
		6.56	g CO2/kg COD	log normal	1.855	0.2272
1	emission of CH4 in WWTP	0.00	y 002/ky 000	log normal	1.000	0.2212
		0.50	g CO2/kg COD	log hormai	1.000	0.2212

Ultra Liquid: Compa	arison situation 3					
				mathematical of	description	
Stage	parameter	mean	unit	distribution	μ	σ
		value			-	

use	washing temperature	30/40	°C	discrete uniform	n.a.	n.a.
	energy use washing machine (a measure of efficiency)	0.0168	kWh/ºC.wash	normal	0.01680	0.005450
	emissions during electricity generation for washing machine	570	g CO2 eq/kWh	log normal	6.326	0.1982
product ingredient production	amount ingredients	Non-disclosed inf	ormation	Non-disclose	d information	
packaging	amount HDPE in package and bulk pack	68.5	g/wash	log normal	4.226	0.04766
production	amount PP in package and bulk pack	10	g/wash	log normal	2.301	0.04766
	amount LDPE in package and bulk pack	0.688888889	g/wash	log normal	-0.3738	0.04766
	amount Corrugate in package and bulk pack	62.85555556	g/wash	log normal	4.140	0.04766
	emission during production HDPE for package and bulk pack	3700	g CO2 eq/package	log normal	8.139	0.3931
	emission during production PP for package and bulk pack	4400	g CO2 eq/package	log normal	8.312	0.3931
	emission during production LDPE for package and bulk pack	2086.3	g CO2 eq/package	log normal	7.566	0.3931
	emission during production Corrugate for package and bulk pack	550.98	g CO2 eq/package	log normal	6.234	0.3931
transport	distance transport raw material, road to port, by truck	500	km	log normal	6.137	0.3931
	distance transport raw material, sea to plant, by ship	100	km	log normal	4.528	0.3931
	distance transport raw material, road to plant, by truck	100	km	log normal	4.528	0.3931
	emissions during transport by truck	107.118	g CO2 eq/ton.km	log normal	4.597	0.3931
	emissions during transport by ship	44.5794	g CO2 eq/ton.km	log normal	3.720	0.3931
formula manufacturing	emissions during formulation compact powder	44	g CO2 eq/kg	log normal	3.707	0.3931
packaging waste treatment	include packaging waste treatment	yes/no	-	discrete uniform	n.a.	n.a.
	fraction recycling of HDPE in package and bulk pack	0.5	-	log normal	-0.7018	0.1312
	fraction recycling of LDPE in package and bulk pack	0.1	-	log normal	-2.311	0.1312
	fraction recycling of Corrugate in package and bulk pack	0.37	-	log normal	-1.003	0.1312

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emissions during landfilling of Corrugate	1198.47	g CO2 eq/package	log normal	7.012	0.3931
emissions during incineration w/o energy recovery of Corrugate	41.1744	g CO2 eq/package	log normal	3.641	0.3931
emissions during incineration with energy recovery of Corrugate	-377.02	g CO2 eq/package	log normal	5.855	0.3931
emissions during landfilling of LDPE	6.15	g CO2 eq/package	log normal	1.739	0.3931
emissions during incineration w/o energy recovery of LDPE	2904.84	g CO2 eq/package	log normal	7.459	0.3931
emissions during landfilling of PP emissions during incineration with energy recovery of LDPE	1874.001	g CO2 eq/package g CO2 eq/package	log normal log normal	1.739 7.459	0.3931
emissions during incineration w/o energy recovery of PP	2904.84 6.15	g CO2 eq/package	log normal	7.897 1.739	0.3931 0.3931
emissions during incineration with energy recovery of PP	1675.48	g CO2 eq/package	log normal	7.347	0.3931
	6.15	g CO2 eq/package	log normal	1.739	0.3931
emissions during incineration w/o energy recovery of HDPE	2904.84	g CO2 eq/package	log normal	7.897	0.3931
emissions during incineration with energy recovery of HDPE	1874.001	g CO2 eq/package	log normal	7.459	0.3931
emissions during recycling of Corrugate in package and bulk pack	576.79	g CO2 eq/package	log normal	6.280	0.3931
emissions during recycling of LDPE in package and bulk pack	56	g CO2 eq/package	log normal	3.948	0.3931
emissions during recycling of HDPE in package and bulk pack	56	g CO2 eq/package	log normal	3.948	0.3931
and bulk pack fraction packaging incineration w/o energy recovery of Corrugate in package and bulk pack	0.001	-	log normal	-6.916	0.1312
fraction packaging incineration with energy recovery of Corrugate in package	0.088	-	log normal	-2.439	0.1312
fraction packaging landfilling of Corrugate in package and bulk pack	0.911	-	log normal	-0.1018	0.1312
bulk pack fraction packaging incineration w/o energy recovery of LDPE in package and bulk pack	0.001	-	log normal	-6.916	0.1312
	0.088	-	log normal	-2.439	0.1312
pack fraction packaging landfilling of LDPE in package and bulk pack	0.911	-	log normal	-0.1018	0.1312
fraction packaging incineration with energy recovery of PP in package and bulk pack fraction packaging incineration w/o energy recovery of PP in package and bulk	0.088	-	log normal	-2.439 -6.916	0.1312
fraction packaging landfilling of PP in package and bulk pack	0.911	-	log normal	-0.1018	0.1312
bulk pack fraction packaging incineration w/o energy recovery of HDPE in package and bulk pack	0.001	-	log normal	-6.916	0.1312
hulls neek			log normal	-2.439	0.1312

waste water treatment

Theo	oretical oxygen demand of ingredients	Non-disclosed information		Non-disclosed information		
elect	tricity use per kg inorganic material in WWTP	0.65	kWh/kg	log normal	-0.5080	0.3931
		0.0211	e e	log normal	-3.936	0.3931
diese	el oil use per kg inorganic material in WWTP	0.011	g/kg	log normal	-4.587	0.3931
elect	tricity use per kg COD organic material in WWTP	0.29	kWh/kg COD	log normal	-1.315	0.3931
natu	ral gas use per kg COD organic material in WWTP	0.0093	cum/kg COD	log normal	-4.755	0.3931
diese	el oil use per kg COD organic material in WWTP	0.005	g/kg COD	log normal	-5.376	0.3931
emis	ssion of CO2 in WWTP	577.2	g CO2/kg COD	log normal	6.332	0.2272
emis	ssion of CH4 in WWTP	6.56	g CO2/kg COD	log normal	1.855	0.2272

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