

1 To what extent is the Circular Footprint Formula of the Product

2 Environmental Footprint Guide consequential?

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4 Dieuwertje L. Schrijvers¹, Philippe Loubet^{1*}, Bo P. Weidema²

5 ¹ Univ. Bordeaux, CNRS, Bordeaux INP, ISM, UMR 5255, F-33400, Talence, France

6 ² Aalborg University, Rendsburggade 14, 9000 Aalborg, Denmark

7 *philippe.loubet@enscbp.fr

8 Abstract

9 With the ambition to increase the comparability of LCA results, the European Commission developed the
10 Product Environmental Footprint (PEF) Guide. This Guide contains a formula to model a product's end-of-
11 life, allowing for waste treatment, energy recovery, and recycling: The Circular Footprint Formula (CFF).
12 The CFF considers the market situation of recycled materials and models recycling via substitution, which
13 is in line with a consequential LCA (CLCA) approach. Therefore, the question that is raised is *"Is the CFF is*
14 *indeed consistent with CLCA, and if not, what are the main differences between the CFF and CLCA*
15 *approaches?"* To facilitate this comparison, a Causal Loop Diagram (CLD) has been developed that
16 summarizes current CLCA practice. From this CLD, a formula has been derived: the market-driven
17 substitution approach, which is compared to the CFF. We conclude that the CFF is partially consistent with
18 a consequential approach. The main discrepancies of the CFF compared to a consequential approach are
19 1) the lack of differentiation between the marginal production processes and users and the specific value
20 chain of the life cycle under study, 2) limitations in the extent to which substitution can be modeled, and
21 3) an incomplete modeling of the effects of recycling when demand is constrained. Furthermore, some
22 parameters in the CFF combine several consequences, which could result in misinterpretations and a lack

23 of transparency of the modeled substitutions. We suggest improvements to the CFF, contributing to
24 harmonizing the application of substitution and the comparability of products assessed according to the
25 PEF Guide.

26 1. Introduction

27 Comparability of LCA results beyond pre-defined studies is an important requirement for consumers to
28 make environmentally informed decisions in the marketplace. However, comparability of results is often
29 limited by the numerous choices that an LCA practitioner can make throughout his or her study. One of
30 these choices having a large impact on the final results is how the end of life of a product is modeled,
31 especially when this product is recycled (Laurent et al., 2014; Merrild et al., 2008). The European
32 Commission has as ambition to develop an LCA approach that can be applied consistently to a large range
33 of products, presented in the Product Environmental Footprint (PEF) Guide (European Commission, 2013).
34 The guidance presented in 2013 included an end-of-life formula, applicable to a wide range of end-of-life
35 scenarios, such as landfilling, energy recovery, and recycling. Environmental burdens and credits due to
36 recycling were equally shared between the producer and the user of the recycled material, following the
37 “50/50 method”. However, this 50/50 method has led to much criticism in the LCA domain. The 50/50
38 method models environmental impacts that are in some cases unrealistic, since it requires that specific
39 waste treatments at the end of life (e.g. by landfilling) be modeled, even if this waste treatment does not
40 take place in reality (Finkbeiner, 2013). Stakeholders in the metals sector argued that the 50/50 method
41 favors incineration over recycling, since the benefits of energy recovery are modeled with 100% credit to
42 the producer of the material. Furthermore, modeling environmental benefits of recycling (by avoiding the
43 primary production of a material) only by 50% is not representative for many metals, since recycling might
44 in some cases substitute primary production by 100% (Eurofer et al., 2013). Also (Schrijvers et al., 2016a)
45 highlighted that the application of the 50/50 method does not consider the different market situations of
46 recycled materials.

47 In response to such criticism and user feedback, the European Commission continued the development of
48 an end-of-life formula for the PEF Guide, and proposed an updated formula in 2016: the Circular Footprint
49 Formula (CFF) (Zampori et al., 2016). The CFF is now integrated into more recent guidance to develop PEF
50 Category Rules (PEFCRs) (European Commission, 2018). The main difference to the 50/50 method is that
51 the environmental burdens and benefits of recycling are now not always equally shared between the user
52 and the producer of the recycled material, but are shared according to a market-parameter *A*. This
53 parameter reflects whether the demand for the recycled material is high or low compared to the
54 production rate. In this way, the CFF resembles the substitution methods that are applied in consequential
55 modeling (Schrijvers et al., 2016b). Therefore, the question that is raised in this paper is whether the CFF
56 is consistent with a consequential LCA approach, and if not, what are the main differences between the
57 CFF and full consequential modeling? It should be noted that the CFF does not explicitly claim to follow a
58 consequential modelling approach. However, answering this question can help to identify whether the CFF
59 can be used outside the scope of the PEF Guide, and whether recycling can lead to environmental
60 consequences that are currently not represented in a Product Environmental Footprint.

61 2. Methods

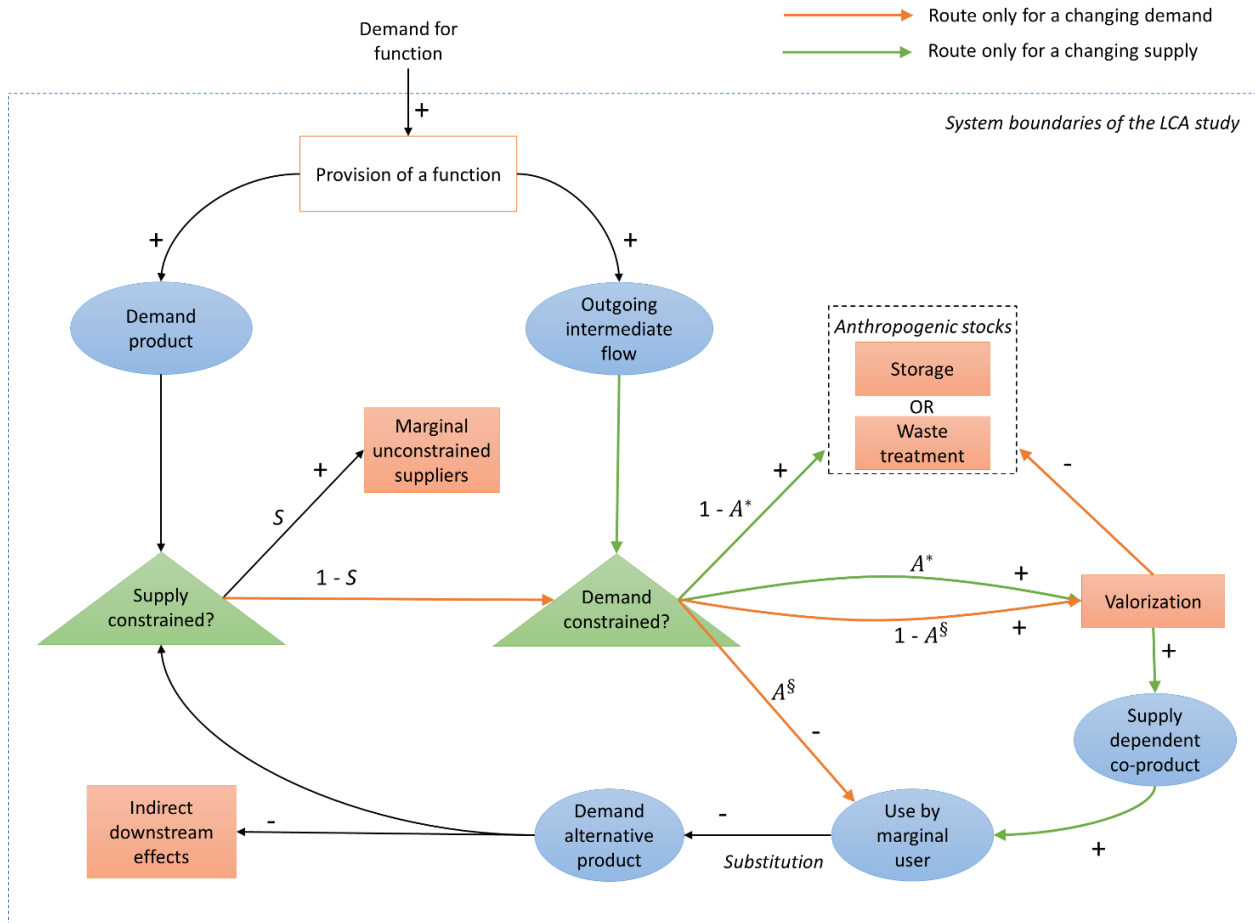
62 The CFF is presented in the form of a formula. In order to evaluate whether the CFF follows a consequential
63 approach, we express the consequential LCA (CLCA) method in the form of a formula as well. The formula
64 for CLCA, which we call “the market-driven substitution method”, is established by first developing a
65 Causal Loop Diagram (CLD) that summarizes the effects that are modeled in a CLCA – covering the
66 application of CLCA as described by Ekvall and Weidema (2004), Weidema et al. (2009), and as
67 implemented in ecoinvent v.3 (Weidema et al., 2013). Subsequently, the elements of the CLD are
68 expressed in mathematical terms. The Supporting Information (SI) provides an illustrative application
69 example of the “market-driven substitution method”. The CFF is presented, and the terms of the CFF are

70 linked to the terms of the market-driven substitution method. This permits to see in detail where the
71 formulas differ or concur. Finally, the differences and their consequences are discussed.

72 3. Results and discussion

73 3.1. A Causal Loop Diagram for modeling a consequential LCI

74 The consequences of a demand for a certain function, which generally leads to the demand for, or supply
75 of, products, can be summarized in a Causal Loop Diagram (CLD) as shown in Figure 1. While CLDs have
76 been used before in the context of CLCA to represent specific effects, such as the rate at which a recycled
77 material can displace a primary material (Zink et al., 2016), the diagram of Figure 1 is comprehensive by
78 visualizing all the effects that must be taken into consideration in the assessment of a changed demand
79 for a function a CLCA.



80
 81 Figure 1 Causal Loop Diagram showing the market-induced consequences of a changing demand for a function. The arrows
 82 reflect causal relationships which can be positive (increased X causes an increased Y; indicated by a plus) or negative (increased X
 83 causes a decreased Y; indicated by a minus). Blue circles refer to flows of material/energy. Green triangles indicate context-
 84 dependent economic factors, which affect the expected consequences. Orange boxes refer to activities that are modeled in the
 85 LCI; each solid filled box represents a set of incoming and outgoing intermediate flows. S represents the level of supply
 86 constraints for a demanded product: $S = 1$ for unconstrained supply, $S = 0$ for fully constrained supply. The green arrows and
 87 A^* represent an outgoing intermediate flow and the orange arrows and A^S represent an incoming intermediate flow: $A^*/S = 1$ for
 88 unconstrained demand, $A^*/S = 0$ for fully constrained demand.

89 3.1.1. Elements of the Causal Loop Diagram

90 **Provision of a function:** The demand for a function leads to a fulfilment of this function, which is can be
 91 considered as a unit process with elementary flows (not indicated in the CLD), incoming product flows,
 92 and outgoing intermediate flows. For example, the demand for the function “obtaining news from a

93 newspaper” has the incoming flow of the demanded newspaper, and the outgoing intermediate flow of
94 the end-of-life newspaper. If the effects of an incoming waste flow need to be modeled, the incoming
95 waste is modeled as a negative outgoing intermediate flow.

96 *Demand product:* The functional unit in a CLCA is often represented by an increasing or decreasing demand
97 for one or more (recycled or primary) products – i.e. the reference flow, which results in a cascade of
98 increased or decreased demands for intermediate flows related to the production of this reference flow.
99 “Demand product” represents one of these increased or decreased demands at a time. The consequences
100 of the changing demand of each product is assessed separately. If a product contains both primary and
101 recycled materials that can be distinguished as such and this is communicated on the market, these are
102 considered to be two separate materials that need to be analyzed independently as well.

103 *Outgoing intermediate flow:* The intermediate flows that result from the provision of the function are
104 modeled as “outgoing intermediate flow”, which contain wastes, materials that need further processing,
105 or dependent co-products, if no further processing is needed (in that case, the LCI of “valorization” could
106 be zero). Outgoing intermediate flows affect marginal valorization, when an economically viable
107 valorization activity exists that transforms the intermediate flow into a dependent co-product for which
108 there is unmet demand. Otherwise, the flow affects marginal waste treatment or storage.

109 *Supply constrained:* The existence of supply constraints determines the first line of consequences of the
110 changing demand for a product. The level of supply constraints is indicated in Figure 1 with the value S . If
111 supply is unconstrained, $S = 1$. If the supply is fully constrained, $S = 0$. The level of supply constraints is
112 often generalized for determining and dependent co-products. A determining co-product is defined as a
113 co-product “for which a change in demand will affect the production volume of the co-producing unit
114 process” (Weidema et al., 2009), and thus not supply constrained. Guidance in the identification of the
115 determining co-product is provided by Consequential-LCA (2015). Generally, it is assumed in LCI, as well

116 as in the ecoinvent 3 database, that the supply of a determining co-product is fully elastic (i.e. $S = 1$)
117 (Weidema et al., 2013), meaning that a change in demand is followed by an equal change in supply. This
118 assumption is valid for competitive markets in the long term (Weidema et al., 2009). For dependent co-
119 products, supply is ultimately constrained by the demand for the determining co-product. Therefore, the
120 default value for recycled products and by-products is $S = 0$.

121 *Marginal unconstrained suppliers:* To the extent that supply is unconstrained, the demand for a product
122 will result in a corresponding increase in production by the marginal supplier.

123 *Demand constrained:* Dependent co-products, either demanded to provide a function, or supplied by a
124 valorization activity, can be in high demand or in low demand, indicated by Parameter A. If the demand
125 for the product is larger than the constrained supply, the demand is unconstrained and $A = 1$. If, however,
126 the market is saturated and an additionally available unit of the product will not be used, demand is
127 constrained and $A = 0$. The situation $0 < A < 1$ may occur in the short term, when markets are affected by
128 short-term constraints, but since a marginal change in demand for a material that is supply constrained
129 does not affect the long-term opportunity costs (the costs of valorization, storage and waste treatment),
130 the long-term situation will tend towards $A=0$, i.e. the entire additional demand will be met by decreasing
131 marginal storage or waste treatment. The situation $0 < A < 1$ may also occur as an average over
132 geographical areas or time periods, where $A=1$ in some subset of geographical areas or time periods, and
133 $A=0$ in other subsets. A changed demand for a product with unconstrained demand (i.e. $A = 1$) affects the
134 use of this product by the marginal user, who can substitute the use of this product by an alternative
135 product. If the demand is however constrained, a changed demand affects the valorization of this product
136 from anthropogenic stocks (i.e. waste or stored materials). A changed supply of an intermediate flow
137 affects either waste treatment/storage, or the valorization of this flow resulting in the production of the
138 dependent co-product, which serves in the determination of A. If there is unmet demand ($A = 1$), the
139 intermediate flow will be valorized and the dependent co-product is used by its marginal user. If the

140 demand is lower than the availability of the intermediate flow ($A < 1$), only waste treatment and storage –
141 not valorization – are affected.

142 *Use by marginal user:* If the demand for a supply-constrained product is not constrained, i.e. if the demand
143 exceeds the constrained supply, the consequence of an additional demand for this product is a reduced
144 use of this supply-constrained product in another product value chain. The marginal user that is affected
145 could be identified by a high elasticity of demand, meaning that a small change in the price of a product
146 will lead to a large change in demand for this product. The user of this product can most easily accept a
147 reduction in use or substitute the supply-constrained product for an alternative material or product that
148 fulfills the same function.

149 *Demand alternative product:* The decreased or increased use of a supply-constrained product in other
150 applications can lead to the increased or decreased demand for an alternative product, respectively – i.e.
151 substitution. This alternative product could be identified by cross-price elasticities of the materials that
152 show whether a change in the price of one product results in a change in demand for the alternative
153 product. Note that this alternative product is the one consumed by the marginal user, which is not
154 necessarily the same user as the operator of the foreground subsystem of the CLCA.

155 *Indirect downstream effects:* Due to the use of an alternative product, indirect effects could take place
156 downstream, in distribution, use, and end-of-life treatment, when the substituted products do not have
157 exactly the same properties. If substitution does not take place on a one-to-one elemental level, but on a
158 product function or technology level, differences in technology efficiencies and system design must be
159 considered as well. Note that, due to the negative causal relation between “demand alternative product”
160 and “indirect downstream effects”, these downstream effects are defined as the downstream inventory
161 related to the product under study *minus* the downstream inventory related to the alternative product.
162 Also rebound effects can be considered within the box “indirect downstream effects”.

163 *Anthropogenic stocks:* Anthropogenic stocks are the marginal supplier of dependent co-products for which
164 demand is less than the supply. If anthropogenic stocks are affected, this is modeled as the storage of the
165 dependent co-products that are not taken into use yet, or as the potential waste treatment of end-of-life
166 products.

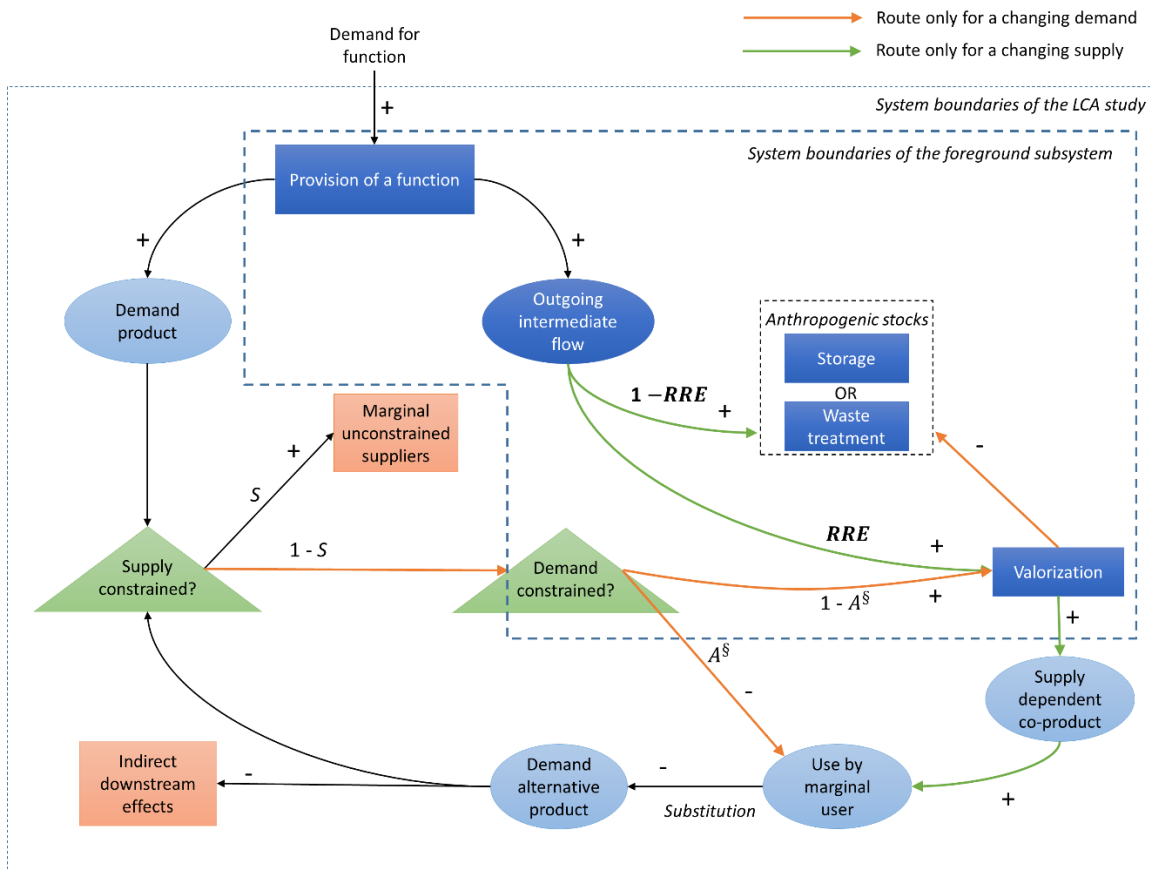
167 *Valorization:* Valorization of a material comprises all activities that take place to make a waste or a co-
168 product a valuable material. This includes sorting and recycling activities, or the incineration activity that
169 is required for energy recovery (energetic valorization).

170 *Supply dependent co-product:* The valorization activity supplies a dependent co-product. Demand
171 constraints (i.e. the determination of A) are identified for this material to evaluate the consequences of a
172 changing supply of an outgoing intermediate flow.

173 3.1.2. *End-of-life recycling rate within the CLD*

174 The CLD shows activities that are likely to take place when an intermediate flow is taken from, or put on
175 the market. It can be noticed that the CLD does not contain a recycling rate – here defined as the share
176 of an outgoing intermediate flow which is sent to a valorization activity. The supply of, or demand for, a
177 material affects valorization via market mechanisms if there is an economically viable valorization
178 activity that supplies a product which is in high demand. Whereas the share of a material flow that is
179 sent to recycling can be determined by players within a value chain (e.g. by the collective action of
180 individuals, through policy, or by a company), the total amount of recycled material (i.e. the supplied
181 dependent co-product) that is finally used in products or applications, and which can substitute a
182 primary material, is determined by market mechanisms. If the amount of material that is sent to
183 valorization within a certain product system is known, the valorization process is modeled within the
184 foreground subsystem – which contains processes that are known to be directly affected by the
185 functional unit, as shown in Figure 2. The dependent co-product that is supplied by the valorization
186 activity is put on the market, and the CLD can be used to model the subsequent effects of this action.

187 The recycled material can be supplied, regardless whether there is a demand for this material. Therefore,
 188 it should be considered that the recycled material produced by the processes within the foreground
 189 subsystem might either substitute a virgin material (if the demand for the recycled material is high), or a
 190 recycled material from other product value chains (if the demand is low). Following the CLD, the node
 191 “demand alternative product” should first be evaluated for recycled materials from other value chains. If
 192 demand is high (i.e. $A = 1$), this recycled material will be increasingly used to substitute a primary
 193 material in a second iteration of consequences. If demand is low ($A < 1$), the valorization and waste
 194 treatment of this alternative recycled material will be affected.



195

196 *Figure 2 Causal Loop Diagram showing the system boundaries of the foreground subsystem with a determined end-of-life*
 197 *recycling rate (RRE) of an outgoing intermediate flow. Processes that are part of the foreground subsystem are indicated by a*
 198 *dark blue color.*

199 3.2. The market-driven substitution method

200 In this section, the effects that are modeled by the CLD of Figure 1 are captured by a mathematical
 201 formula. The SI presents an example illustrating the link between the CLD and the formula. To enable the
 202 comparison with the CFF in Section 3.4, the market-driven substitution formula is presented in a modular
 203 form in Equations E1-E4. Whereas each input and output material should be modeled separately in a
 204 CLCA, Equation E2 reflects a combined case where one primary material and one recycled material are
 205 used, and where one recycled material is supplied at the end of life, which may or may not be the same
 206 as the consumed recycled material. The parameters of the formula are given in Table 1.

207 E1. $E_{tot} = E_{tot,material} + E_{tot,energy} + E_{tot,disposal}$

208 E2. $E_{tot,material} = (1 - RC) * E_v + RC * \left((1 - A^S) * \left(E_r^S - \frac{E_d^S}{C^S} \right) - A^S * \frac{Q^S}{Q_v^S} * (\Delta E_\alpha^S - E_v^S) \right) + RRE_{rec} *$

209 $C_{rec} * \left(E_{r,rec} - (1 - A^*) * \left(E_r^* - \frac{E_d^*}{C^*} \right) + A^* * \frac{Q^*}{Q_v^*} * (\Delta E_\alpha^* - E_v^*) \right)$

210 E3. $E_{tot,energy} = RRE_{inc} * (E_{RRE,inc} - C_{elec} * E_v^*)$

211 E4. $E_{tot,disposal} = (1 - RRE_{inc} - RRE_{rec}) * E_d$

212 Table 1 Explanation of terms of the market-driven substitution method presented in Equations E2-E5

Term of the market-driven substitution method	Explanation	Value
E_{tot}	Life Cycle Inventory (LCI) caused by the demand for the product under study via a consequential LCA	LCI / unit of analysis

E_v	LCI caused by the extraction and processing of primary (virgin) materials via the marginal production process (including processing inefficiencies)	LCI / unit of primary material
$E_v^{\$}$	LCI caused by the extraction and processing of the primary (virgin) materials that are substituted by the marginal user of the demanded material (including processing inefficiencies)	LCI / unit of primary material
E_v^*	LCI caused by the extraction and processing of the primary (virgin) materials that are substituted by the marginal user of the supplied material (including processing inefficiencies)	LCI / unit of primary material
$E_{r,rec}$	LCI caused by the production of the supplied recycled material (including LCI of losses during the recycling process)	LCI / unit of produced recycled material
$E_r^{\$}$	LCI caused by the production of the demanded recycled material via the marginal valorization process (including LCI of losses during the recycling process)	LCI / unit of produced recycled material
E_r^*	LCI caused by the production of the supplied recycled material via the marginal valorization process (including LCI of losses during the recycling process)	LCI / unit of produced recycled material
$E_{RRE,inc}$	LCI caused by the incineration of the end-of-life product (including LCI of losses during the recovery process)	LCI / unit of incinerated end-of-life product

E_d	LCI caused by waste treatment or storage	LCI / unit of discarded or stored material
E_d^S	LCI caused by the waste treatment or storage of the demanded recycled product via the marginal treatment process	LCI / unit of discarded or stored material
E_d^*	LCI caused by the waste treatment or storage of the supplied recycled product via the marginal treatment process	LCI / unit of discarded or stored material
$\frac{Q^S}{Q_v^S}$	Quantity-correction factor that indicates the amount of a primary material that is substituted by the demanded recycled material by its marginal user	Unit of substituted primary material / unit of recycled material
$\frac{Q^*}{Q_v^*}$	Quantity-correction factor that indicates the amount of a primary material that is substituted by the supplied recycled material by its marginal user	Unit of substituted primary material / unit of recycled material
ΔE_α^S	LCI due to additional (+) and/or decreased (-) downstream intermediate or elementary flows related to the distribution, use, and disposal of the recycled material instead of a primary material by the marginal user of the demanded recycled material	LCI / unit of substituted primary material
ΔE_α^*	LCI due to additional (+) and/or decreased (-) downstream intermediate or elementary flows related to the distribution, use, and disposal of the recycled material instead of a primary material by the marginal user of the supplied recycled material	LCI / unit of substituted primary material

RC	Recycled content (recycled or recovered material input per unit of analysis)	$0 \leq RC \leq 1$
RRE_{rec}	End-of-life recycling rate (share of the product at the end of life that is sent to recycling)	$0 \leq RRE_{rec} \leq 1$
RRE_{inc}	End-of-life incineration rate (share of the product at the end of life that is sent to incineration)	$0 \leq RRE_{inc} \leq 1$
C_{rec}	Conversion efficiency of the end-of-life product into a recycled material	Unit of useful output / unit of input material
C_{elec}	Conversion efficiency of the end-of-life product into recovered electricity	Unit of useful output / unit of input material
C^{\S}	Conversion efficiency of the end-of-life product into a recycled material via the marginal valorization process of the demanded recycled material	Unit of useful output / unit of input material
C^*	Conversion efficiency of the end-of-life product into a recycled material via the marginal valorization process of the supplied recycled material	Unit of useful output / unit of input material
A^{\S}	Indicator for demand constraints of the used recycled material ($A^{\S} = 0$ reflects fully constrained demand; $A^{\S}=1$ reflects fully unconstrained demand)	$0 \leq A^{\S} \leq 1$
A^*	Indicator for demand constraints of the supplied recycled material ($A^* = 0$ reflects fully constrained demand; $A^*=1$ reflects fully unconstrained demand)	$0 \leq A^* \leq 1$

214 3.3. Circular Footprint Formula

215 The European Commission (European Commission, 2018; Zampori et al., 2016) proposed a Circular
 216 Footprint Formula (CFF) to replace the End-of-Life formula of the PEF Guide (European Commission, 2013).
 217 The latest version of this formula shows similarities with the formulas provided in Section 3.2 of this paper.
 218 The CFF is a combination of three equations that calculate the impacts and benefits related to the use and
 219 supply of materials, the recovery of energy, and disposal (Equations E6-E9). The terms of these equations
 220 are explained and compared with the terms of the market-driven substitution method in Table 2.

221 E5. $CFF_{total} = CFF_{material} + CFF_{energy} + CFF_{disposal}$

222 E6. $CFF_{material} = (1 - R_1) * E_v + R_1 * \left(A_{CFF} * E_{recycled} + (1 - A_{CFF}) * E_v * \frac{Q_{Sin}}{Q_P} \right) + (1 - A_{CFF}) * R_2 * \left(E_{recyclingEoL} - E_v^* * \frac{Q_{Sout}}{Q_P} \right)$

224 E7. $CFF_{energy} = (1 - B) * R_3 * (E_{ER} - LHV * X_{ER,heat} * E_{SE,heat} - LHV * X_{ER,elec} * E_{SE,elec})$

225 E8. $CFF_{disposal} = (1 - R_2 - R_3) * E_d$

226 Table 2 Terms of the Circular Footprint Formula and their equivalence with the terms of the market-driven substitution formula

Term of the CFF	Explanation (European Commission, 2018)	Equivalent term of the market-driven substitution method
CFF_{total}	Life Cycle Inventory (LCI) caused by the demand for the product under study via the Circular Footprint Formula	E_{tot}
A_{CFF}	Allocation factor of burdens and credits between supplier and user of recycled materials	$(1 - A^S)$ and $(1 - A^*)$
B	Allocation factor of energy recovery processes: it applies both to burdens and credits	$(1 - A^*)$

Q_{Sin}	Quality of the ingoing secondary material, i.e. the quality of the recycled material at the point of substitution	Q^S
Q_{Sout}	Quality of the outgoing secondary material, i.e. the quality of the recyclable material at the point of substitution	Q^*
Q_P	Quality of the primary material, i.e. quality of the virgin material	Q_v^S and Q_v^*
R_1	Proportion of material in the input to the production that has been recycled from a previous system	RC
R_2	Proportion of the material in the product that will be recycled (or reused) in a subsequent system. R2 shall therefore take into account the inefficiencies in the collection and recycling (or reuse) processes. R2 shall be measured at the output of the recycling plant	$RRE_{rec} * C_{rec}$
R_3	Proportion of the material in the product that is used for energy recovery at EoL	RRE_{inc}
$E_{recycled}$	Specific emissions and resources consumed (per functional unit) arising from the recycling process of the recycled (reused) material, including collection, sorting and transportation process	E_r^S
$E_{recyclingEoL}$	Specific emissions and resources consumed (per functional unit) arising from the recycling process at EoL, including collection, sorting, and transportation process	$E_{r,rec}$ and E_r^*

E_v	Specific emissions and resources consumed (per functional unit) arising from the acquisition and pre-processing of virgin material	E_v and E_v^S
E_v^*	Specific emissions and resources consumed (per functional unit) arising from the acquisition and pre-processing of virgin material assumed to be substituted by recyclable materials	E_v^* (if $E_v^S = E_v^*$) or $E_v^* * \frac{Q^*}{Q_v^*}$ (if $E_v^S \neq E_v^*$)
E_{ER}	Specific emissions and resources consumed (per functional unit) arising from the energy recovery process (e.g. incineration with energy recovery, landfill with energy recovery, ...)	$E_{RRE,inc}$
$E_{SE,heat}$ and $E_{SE,elec}$	Specific emissions and resources consumed (per functional unit) that would have arisen from the specific substituted energy source, heat and electricity respectively	E_v^*
E_d	Specific emissions and resources consumed (per functional unit) arising from disposal of waste material at the EoL of the analysed product, without energy recovery	E_d
$X_{ER,heat}$ and $X_{ER,elec}$	The efficiency of the energy recovery process for both heat and electricity	C_{heat}^1 and C_{elec}
LHV	Lower Heating Value of the material in the product that is used for energy recovery	

¹ In our formula for the market-driven substitution method there is no explicit parameter for recovered heat, but this would be calculated in the same way as for recovered electricity.

228 3.4. Comparison of the Circular Footprint Formula with the market-driven substitution
229 method

230 The differences and similarities between the CLCA method (via the market-driven substitution method)
231 and the CFF are identified, term by term, in Table 3. The main differences and their consequences are
232 discussed below.

233 3.4.1. *Marginal processes and marginal users*

234 In CLCA, processes in the background subsystem are marginal production and treatment processes, while
235 this is not an explicit requirement in the CFF. Therefore, the LCA practitioner applying the CFF might select
236 a production or treatment process that is different from the marginal process. The CFF would only be
237 consistent with the CLCA approach when all the processes within the value chain of the product under
238 study are also the marginal processes.

239 The primary material that is used in the product under study (E_p in the market-driven substitution method)
240 is not necessarily the same as the primary material that is used by the marginal user of this recycled
241 material. This is taken into account in the CFF by the substitution of an alternative primary material,
242 denoted as E_p^* , by the supplied recycled material. However, this is not considered for the recycled content.
243 This can be, for example, relevant when the recycled material is “upcycled” (substituting a high-value
244 primary material) in the application under study, whereas it would otherwise be “downcycled”
245 (substituting a low-value primary material) by the marginal user (see the example in the SI). In the CFF, it
246 would be assumed that the marginal user substitutes the same primary material as the user in the
247 foreground subsystem. Consequently, the CFF does not consider any other downstream effects that the
248 marginal user experiences when switching back to a primary alternative instead of using the recycled
249 material (i.e. the use of additives in the example of the SI). The lack of differentiation between the primary
250 material in the life cycle under study and the primary material used by the marginal user of the recycled

251 material and the lack of inclusion of downstream effects are only justified in the specific situation where
252 the life cycle under study represents the marginal user of the recycled material.

253 3.4.2. *Factor A and Factor B*

254 The A-factor of the CFF represents, similar to the A-factors of the market-driven substitution method, the
255 market situation of the recycled material. However, there are differences between the CFF and the
256 market-driven substitution method in how A is determined and what consequences are considered to take
257 place, depending on the market-situation of a recycled material.

258 In the CFF, if there is a low offer of the recycled material and a high demand, $A_{CFF} = 0.2$. If there is a high
259 offer of the recycled material and a low demand, $A_{CFF} = 0.8$. A_{CFF} can never have a value of 0 or 1, hence,
260 full substitution is never an option. The European Commission provides a list of A-values for different
261 materials, such as metals, paper, plastics, glass and wood, which is established and updated by the
262 European Commission (European Commission, 2018). Freedom to determine A based on the context at
263 hand could be preferable as different material grades, locations or contexts could provide different
264 demand constraints. Besides, this could allow for the modeling of full substitution by enabling values of 0
265 and 1. Moreover, the CFF does not distinguish between demand constraints of the consumed recycled
266 material and demand constraints of the produced recycled material, while two separate terms for this
267 exist in the CLCA method. As shown in the example of the SI for CLCA, the consumed recycled materials
268 do not necessarily have the same market situation as the supplied recycled materials, which is especially
269 relevant in the case of open-loop recycling.

270 Regarding the consequences that are modeled via Factor A, the CFF considers that the demand for a
271 recycled material might be low, and that the additional demand or the additional supply for a recycled
272 material with low demand leads to additional or decreased recycling of this material, respectively.
273 However, the CFF does not consider that this additional or decreased recycling could lead, in turn, to

274 avoided or increased waste treatment, respectively, while this consequence is included in the market-
275 driven substitution method.

276 Energy recovery is not represented by an *A*-factor, but instead by a Factor *B*. In contrast to the input of
277 recycled material, the input of recovered energy is not included in the formula. This is not necessarily a
278 problem, as the default value for *B* for recovered energy is 0. However, if this value would be different,
279 the use of recovered energy should be modeled as well, similar to the recycled content of materials. The
280 equation of the CFF does not include a term for this.

281 3.4.3. Quality correction

282 The CFF integrates quality ratios for the recycled content and the end-of-life recycling rate. This quality
283 ratio of the CFF is determined by the price ratio of the secondary compared to the primary material. The
284 market-driven substitution method does not model the relative quality of the recycled material. Instead,
285 a factor is included that reflects the *quantity* of the primary material that is displaced by the recycled
286 material. The price ratio as used in the CFF could give a misinformed view on the relative quality of a
287 material, because the price ratio can be based on several other considerations, such as substitution in
288 different market segments, downstream effects, or demand constraints. The use of a physical parameter
289 in the market-driven substitution method ensures the mass balance of the resulting inventory, which is
290 not ensured in the CFF.

291 In the case of open loop recycling (when $E_v \neq E_v^*$ in the CFF, or $E_v^{\S} \neq E_v^*$ in the market-driven substitution
292 method), the quality factor is omitted from the CFF, because the parameter E_v^* should reflect “*how much,*
293 *how long, [and] how well*” the recycled material substitutes a primary material (European Commission,
294 2018). However, E_v^* as defined by the CFF in Table 2 only refers to the primary materials that are
295 substituted, and does not explicitly mention any changes during transport, the use phase, or the end-of-
296 life disposal due to the substitution. In the market-driven substitution method, the parameter E_v^* only

297 reflects the specific inventory of the substituted primary production process. The quantity correction
298 factor $\left(\frac{Q^*}{Q_v^*}\right)$ represents “how much” is substituted, and an additional term for indirect downstream effects
299 (ΔE_a^*) is included that represents “how long and how well”, including differences in other life cycle stages.
300 The ambition to include all such effects into a single term in the CFF has as a risk that downstream effects
301 are not systematically taken into consideration, as the LCA practitioner could be contented with the
302 identification of a single raw material without posing further questions.

303 *3.4.4. Calculation of the end-of-life recycling rate*

304 The CFF calculates the end-of-life recycling rate as the output material flow from the recycling process,
305 and recycling inefficiencies are part of the LCI of the recycling process ($E_{recyclingEoL}$). However, the
306 expression of $CFF_{disposal}$ (Equation E8) considers the waste treatment of recycling inefficiencies as well,
307 which are, therefore, double counted. To illustrate this, imagine that 5 kg of plastic waste is treated by a
308 recycling process, with the output of 3 kg of recycled plastic. The 2 kg of plastic waste generated during
309 the recycling activity are modeled in $E_{recyclingEoL}$, and the recycling rate R_2 is defined as 60%. Following
310 Equation E8, final disposal is modeled for $1-R_2$, i.e. 40%, which reflects the same quantity of waste disposal
311 that is already covered by $E_{recyclingEoL}$.

312 *3.4.5. Overall assessment of the CFF*

313 The comparison between the CFF and the market-driven substitution method in Table 3 shows that,
314 despite the large overlap between the two formulas, the CFF does not follow a full consequential method.
315 The main difference lies in the fact that the CFF does not explicitly refer to the marginal production and
316 treatment processes and marginal users of recycled materials. Another difference is the consideration of
317 (avoided) waste treatment when the demand for a recycled material is constrained. This factor was
318 included in the previous version of the CFF (the 50/50 method (European Commission, 2013)) and
319 eliminated from the CFF to simplify the approach. Other discrepancies between the CFF and the market-

320 driven substitution method might also be the result of simplifying choices – such as the predetermined
321 values for A_{CFF} . This paper contributes in highlighting the consequences of such simplifications and
322 providing alternative modeling options that could be applied in sensitivity analyses.

323 As stated above, the CFF does not explicitly claim to follow a consequential modelling approach. The PEF
324 Guide could be seen as a mix between an attributional and a consequential LCA approach (European
325 Commission, 2013). Whether such a mix is desirable has been discussed in other papers (Schrijvers et al.,
326 2016a). Even if a consequential approach is not pursued, the comparison of this article could inspire
327 method developers and users to consider whether their method is in line with the objective of the method.
328 Furthermore, a few inconsistencies were highlighted that merit being checked by the European
329 Commission for future use of the CFF, regarding the quality correction factor and the calculation of the
330 end-of-life recycling rate.

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#	Modeled in CLCA	Term CLCA	Term CFF	CFF expressed in terms of CLCA	Difference
1	Production of primary materials by the marginal production process	$+(1 - RC) * E_v$	$+(1 - R_1) * E_v$	$+(1 - RC) * E_v$	CFF does not specify that E_v represents the marginal process
2	Production of the demanded recycled material by the marginal valorization process, to the extent that the demand for the recycled material is constrained	$+RC * (1 - A^S) * E_r^S$	$+R_1 * A_{CFF} * E_{recycled}$	$+RC * (1 - A^S) * E_r^S$	<ul style="list-style-type: none"> - General differences regarding the factor A, see text - CFF does not specify that E_r^S represents the marginal process
3	Avoided waste disposal or storage of the demanded recycled material by the marginal treatment process, to the extent that the demand for the recycled material is constrained	$-RC * (1 - A^S) * \frac{E_d^S}{C^S}$	NA	NA	- Consequence not considered in the CFF

4	<p>Avoided downstream effects for the marginal user related to the use of the demanded recycled material instead of an alternative material, to the extent that the demand for the recycled material is unconstrained</p>	$-RC * A^S * \frac{Q^S}{Q_v^S}$ $* \Delta E_\alpha^S$	NA	NA	<p>- Consequence not considered in the CFF</p>
5	<p>Production of an alternative material for the marginal user of the demanded recycled material, to the extent that the demand for the recycled material is unconstrained.</p>	$+RC * A^S * \frac{Q^S}{Q_v^S}$ $* E_v^S$	$+R_1 * (1 - A_{CFF})$ $* \frac{Q_{Sin}}{Q_P} * E_v$	$+RC * A^S * \frac{Q^S}{Q_v^S}$ $* E_v$	<p>- General differences regarding the factor A, see text</p> <p>- General differences regarding the quality correction factor, see text</p> <p>- CFF does not differentiate between E_v^S (production of an alternative material for the marginal user of the recycled material) and E_v (production of a primary material for the life cycle under study)</p>

6	Production of the supplied recycled material via the recycling process within the foreground subsystem	$+RRE_{rec} * C_{rec} * E_{r,rec}$	$+R_2 * E_{recyclingEoL}$	$+RRE_{rec} * C_{rec} * E_{r,rec}$	- No difference between CLCA and CFF.
7	Avoided valorization of recycled materials by the marginal valorization process, to the extent that the demand for the supplied recycled material is constrained	$-RRE_{rec} * C_{rec} * (1 - A^*) * E_r^*$	$-R_2 * A_{CFF} * E_{recyclingEoL}$	$-RRE_{rec} * C_{rec} * (1 - A^*) * E_{r,rec}$	- General differences regarding the factor A, see text - CFF does not differentiate between E_r^* (valorization of the recycled material via the marginal process) and $E_{r,rec}$ (valorization of the recycled material via the process in the foreground subsystem).
8	Waste disposal or storage of recycled materials from other product value chains by the marginal disposal process to the extent that the demand for the	$+RRE_{rec} * C_{rec} * (1 - A^*) * \frac{E_d^*}{C^*}$	NA	NA	- Consequence not considered in the CFF

	supplied recycled material is constrained				
9	Downstream effects for the marginal user related to the use of the supplied recycled material instead of an alternative material, to the extent that the demand for the recycled material is unconstrained	$+RRE_{rec} * C_{rec}$ $* A * \frac{Q^*}{Q_v} * \Delta E_{\alpha}^*$	NA	NA	- Consequence not considered in the CFF, although certain of these factors might be covered by the term E_v^* (see Section 3.4.4.)
10	Avoided production of an alternative material for the marginal user of the supplied recycled material, to the extent that the demand for this recycled material is unconstrained.	$-RRE_{rec} * C_{rec}$ $* A * \frac{Q^*}{Q_v} * E_v^*$	$-R_2 * (1 - A_{CFF})$ $* \frac{Q_{Sout}}{Q_P} * E_v^*$	$-RRE_{rec} * C_{rec}$ $* A * \frac{Q^*}{Q_v} * E_v^*$	<ul style="list-style-type: none"> - General considerations regarding the factor A, see text - General considerations regarding the quality correction factor, see text

11	<p>Incineration process within the foreground subsystem</p>	$+RRE_{inc}$ $* E_{RRE,inc}$	$+(1 - B) * R_3$ $* E_{ER}$	$+RRE_{inc}$ $* E_{RRE,inc}$	<p>- The extent to which incineration is modeled in the CFF depends on the factor B. The default value for B is 0, resulting in modeling of the same LCI in CLCA and CFF. If a different value for B would be authorized, the CFF would decrease the LCI of the incineration process.</p>
12	<p>Avoided production of conventional electricity by the marginal production process</p> <p><i>Key assumptions:</i></p> <ul style="list-style-type: none"> - Demand for electricity is unconstrained - No indirect effects take place by using recovered 	$- RRE_{inc} * C_{elec}$ $* E_v^*$	$-(1 - B) * R_3$ $* LHV * X_{ER,elec}$ $* E_{SE,elec}$	$- RRE_{inc} * C_{elec}$ $* E_v^*$	<p>- The extent to which incineration is modeled in the CFF depends on the factor B. The default value for B is 0, resulting in modeling of the same LCI in CLCA and CFF. This corresponds to the key assumption that the demand for electricity is unconstrained.</p>

	<p>instead of conventional electricity</p> <ul style="list-style-type: none"> - 1 MJ of recovered electricity substitutes 1 MJ of conventional electricity 				<ul style="list-style-type: none"> - CFF does not specify the other key assumptions, which is, in the case of recovered energy, acceptable - CFF contains a specific term for recovered heat. As heat and electricity are modeled in the same way in CLCA, heat is not separately specified in the market-driven substitution method
13	Waste disposal process within the foreground subsystem	$+(1 - RRE_{rec} - RRE_{inc}) * E_d$	$+(1 - R_2 - R_3) * E_d$	$+(1 - RRE_{rec} * C_{rec} - RRE_{inc}) * E_d$	<ul style="list-style-type: none"> - In the CFF, R_2 is measured at the output of the recycling process, while in CLCA, RRE_{rec} represents the input flow of the recycling process. The definition of R_2 in the CFF suggests that waste disposal is calculated for both the share of the material that is not recycled, as well as for

					<p>inefficiencies of the recycling process.</p> <p>Recycling inefficiencies are also included in $E_{recyclingEoL}$, and are therefore double counted.</p>
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336 4. Conclusions and perspectives

337 The recently presented Circular Footprint Formula (European Commission, 2018) has been developed to
338 model recycling in LCA in order to make Product Environmental Footprints comparable. The CFF integrates
339 the criticism that was raised after presenting the 50/50 method in the first version of the Product
340 Environmental Footprint Guide (European Commission, 2013), such as the consideration of the market
341 situation of recycled materials. As the CFF models recycling by substitution, a modeling technique that is
342 often associated with consequential LCA, in this paper the question is raised to what extent the CFF is in
343 line with a consequential approach. In order to investigate this, the effects that are generally modeled in
344 a consequential LCA (CLCA) are expressed in the form of a formula, comparable to the CFF.

345 In the process of establishing this formula for CLCA, the causal relationships that are modeled in a CLCA
346 have been visually presented in the form of a Causal Loop Diagram. This demonstrates the added value of
347 the CLCA, as it stimulates the development of a complete LCI without imposing *ex ante* cut-off criteria of
348 potential consequences. The CLD that is presented in this paper can be used as a tool to identify the
349 consequences of a changing demand for a product.

350 The differences between the market-driven substitution method and the CFF of the European Commission
351 demonstrate that the CFF has the potential to, but at the moment does not provide a full consequential
352 approach. Main discrepancies between the CFF and the market-driven substitution method are 1) the lack
353 of differentiation between the marginal supplier and marginal user of materials on the one hand, and the
354 specific value chain of the life cycle under study on the other hand, 2) predetermined limitations to the
355 extent that substitution can be modeled, and 3) an incomplete modeling of the effects of recycling when
356 demand is constrained. Furthermore, combining several effects into a single parameter, such as a single
357 market parameter for both the recycled content and the end-of-life recycling rate, the unclear
358 differentiation between the material entering and exiting a recycling process, and lumping together the

359 LCI of the substituted primary material, quality correction, and other indirect effects could result in
360 misinterpretations and a lack of transparency of the modeled substitutions.

361 These missing specifications, lacking or predetermined parameters, and lack of freedom to interpret the
362 method to the context at hand, imply that the outcome of the CFF can be significantly different than the
363 outcome of the CLCA approach, depending on the experience and rigor of the LCA practitioner. However,
364 the CFF is an improvement compared to the End-of-Life formula of the PEF Guide (European Commission
365 2013) due to a consideration of the recycled material markets (Schrijvers et al., 2016a). Further
366 improvement of the CFF could be achieved by explicitly integrating the differences that are highlighted in
367 this paper, so that the consequences of using or producing a recycled material are more systematically
368 assessed. Such guidance should not be integrated in industry-specific PEFCRs, but rather in an overarching
369 PEF document, as open-loop recycling could lead to material and energy exchanges among different
370 industries. Integrating the suggested improvements would contribute to the harmonization of the
371 application of substitution and the comparability of products assessed according to the PEF Guide.

372 [Supporting Information](#)

373 The Supporting Information contains an illustrative example to demonstrate the link between the Causal
374 Loop Diagram and the market-driven substitution method.

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